## Ways & Rails for Slipways for Dry Docking Ships by Keith Mackie<sup>1</sup>

## 1. ABSTRACT

The slipway is the oldest method of dry docking ships. However, at least for more remote sites without heavy demand, even at the present levels of development, they are the most practical and economic system. With proper development of the technology, they can exceed other systems in these aspects.

The slipway, however is the most technically complex of all forms of dry docking and this complexity is not well understood – if it is recognised at all. As a result, it has remained the 'Cinderella' of the industry.

The discussions in this paper are intended to remedy this situation – to expose and illuminate this complexity, provide a basic design guide and show the way to further investigations.

## 2. BACKGROUND

## 2.1. Origins of the Slipway

There are two basic types of dry docks in use: the hydraulic systems of graving docks and floating docks and the mechanical systems, of which the slipway forms part together with shiplifts and straddles. It is based on the use of the inclined plane and is the oldest form of dry docking. In the 20<sup>th</sup> century, the development of the slipway has lagged behind developments in other forms of dry docking. However, when modern technology is brought to bear, the slipway can be the safest and most efficient method of dry docking. In areas of lower demand, for vessels under 1000 tons docking displacement but even up to 5000 tons the slipway can be the most economical system

In the beginning, when vessels were small, they were just hauled up and down the beach – Fig 1 and Fig 2 and from this the slipway developed – Fig 3 and Fig 4.





Fig 1: Beaching, Soalara, Madagascar 2012 Fig 2: Beaching, Vilanculos, Mozambique, 2009

The formal slipway probably first came into use in the Mediterranean and for thousands of years<sup>2</sup> the slipway consisted of a sled of heavy timber runners over timber sleepers laid on the beach. Some of these are still in use.

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<sup>&</sup>lt;sup>2</sup> At least as far back as the Late Bronze Age



Fig 3: Shipsled, Bosphorus, 2010



Fig 4: Shipsled, Chania, Crete, 1986

#### 2.2. Types of Slipway

The slipway in its modern form of a cradle on wheels on rails can be precisely dated to the patent awarded to Thomas Morton of Leith in 1819 (Prosser R.B.1894) and his system came to be known as a 'patent slipway'. The cradles were built of timber baulks with small cast iron wheels set in wheel boxes under the longitudinal baulks. These facilities were always built to the three-way system so that the whole weight of the vessel was carried on the centre, keel way. The outrigger ways were for lateral stability.



Fig 5: Patent Slip Cape Town c 1920



Fig 6: Crandall Railway Dry Dock

In the mid-19<sup>th</sup> century the Crandall family of Boston, Massachusetts (Crandall 1967) developed their own peculiar system commonly referred to as a 'marine railway' or 'railway dry dock'. They use live rollers instead of wheels and cradles built up aft to a wedge shape so that the line of the keel blocks is level.

During the 20<sup>th</sup> century steel cradles began to replace timber although in general, the three-way system was retained. The modern trend, however, is to exploit the strength of steel and move to a two-way system where the keel block loads are suspended between the two ways by transverse steel cradle beams.



Fig 7: Modern Slipway, Lamberts Bay, South Africa, 1990

## 3. WAYS GEOMETRY

Slipways can be laid out as either end haul or side haul. End haul systems have a greater extent into the water area but a much smaller extent along the shoreline. Side haul systems have a relatively short extent into the water – and a concomitant steeper grade – but a much greater extent along the shoreline.

Side haul slipways have a series of parallel ways, normal to the shore, spaced along the length of the cradle, transverse to the cradle.

With end haul slipways the ways are again normal to the shore but parallel to the cradle. They commonly use either two or three ways although more can be used. In the case of a four-way system, the central, keel way is split into two parallel ways a short distance apart. Rails are fixed to the ways, usually a single rail to the outriggers but, on larger systems two rails to the keel way.

Given that the ways profile is never perfect, there is a better load distribution to the ways on a two-way system than on a three-way system and, to a lesser extent, on four-way systems. Given that slipway cradles are unsprung, accuracy in vertical alignment of the ways is paramount and the spreading of the keel load to ways set apart does assist in the load distribution.

Gradient of the ways usually varies from about 1:10 for very small units to about 1:25 for very large units. At the very flat grades some form of downhaul will usually be necessary. The usual grades lie between 1:15 to 1:20.

## 3.1. Straight Grade Ways



Fig 8: Straight Grade Ways Geomentry

The geometry of the straight grade ways as shown in figure 8 is pretty intuitive and is given for completeness. Given:

*c* = chainage measured horizontally

- $c_1$  = chainage at landward end of ways
- $c_2$  = chainage at seaward end of ways
- $h_c$  = level of ways at chainage c

 $d_f$  = draft fore

- $h_1$  = level at landward end of ways  $h_2$  = level at seaward end of ways
- $i_b$  = tan of angle between line of blocks and ways

 $i_{W}$  = grade of ways as tangent of slope

 $L_c$  = length of cradle over blocks

 $h_r$  = vertical height of reference block above ways

- $F_b$  = freeboard above tide
  - $T = \max$  tide range from LAT to HAT

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d_a = draft aft
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t = stage of tide

Note: the 'reference block' refers to the foremost keel block on the front of the cradle

Level,  $h_c$  at any chainage c:

$$h_c = h_1 + i_w (c_1 - c_2) \tag{1}$$

Chainage *c* at any level *h<sub>c</sub>*:

$$c = c_1 + \frac{h_1 - h_2}{i_W}$$
(2)

Horizontal extent of the ways:

$$c_2 - c_1 = \frac{1}{i_w} \left( F_b + T + h_r + d_f - q \cdot i_b \right) + 2 \cdot L_c \cdot \cos \tan^{-1} i_b \tag{3}$$

Total slope length of the ways:

$$L_{w} = \frac{c_{2} - c_{1}}{\cos \tan^{-1} i_{w}} \tag{4}$$

# Remember: longitudinal dimensions on the cradle are slope dimensions and do not correlate directly with the horizontal chainage dimensions on the ways!

#### 3.2. Vertically Curved Ways



Fig 9: Vertically Curved Ways

Vertically curved ways as shown in **Fig 9**, can make a significant cost saving on the construction of a slipway and improve the operation of the facility. The curve shortens the total length of the ways, reduce the grade of the ways at the landward end and reduces the amount of any rock excavation by bending the ways over the rock.

The computation of the circular curve is complicated by the need to compute the versines (1-cosine) of small angles. It is only with the advent of modern computers that this has become practical.

To determine a suitable ways profile - position and curvature - by trial and error – first establish a site co-ordinate system. Use Chart Datum as the vertical datum, the orientation of the ways as the longitudinal datum and a transverse datum some distance inshore of the proposed ways. The crown of the curve is unlikely to be near the origin of the co-ordinate system. The site will generally suggest initial values. The geometry is shown in **Fig 10**.

For each trial, choose:

Chainage at landward end	<b>C</b> <sub>1</sub>	Gradient at landward end	i1
Chainage at seaward end,	<b>C</b> <sub>2</sub>	Chord length between ref block and end of cradle	Lc
Level at landward end,	h1 (usually +ve)	Angle of build-up of keel blocks	$\pmb{\phi}_b$
Level at seaward end,	<i>h</i> <sub>2</sub> (usually -ve)		





Now compute the following:

$$\alpha_1 = \tan^{-1} i_1 \tag{5}$$

$$\alpha_2 = 2 \tan^{-1} \frac{n_1 - n_2}{c_1 - c_2} - \alpha_1 \tag{6}$$

Grade of seaward end:  $i_2 = \tan \alpha_2$  (7)

Curve radius: 
$$R = \frac{h_1 - h_2}{\cos \alpha_1 - \cos \alpha_2}$$
(8)

$$x_0 = R.\sin\alpha_1 - c_1 \tag{9}$$

Height of crown:  $h' = h_1 + R. (1 - \cos \alpha_1)$  (10)

For construction, compute:

Arc length ch  $c_1$  to ch c:

Crown to origin:

Level at ch c: 
$$h_c = h' - R(1 - \cos \sin^{-1} \frac{x_0 + c}{R})$$
 (11)

$$A_c = R\left(\sin^{-1}\frac{x_0+c}{R} - \alpha_1\right) \tag{12}$$

(13)

Gradient at ch c: 
$$i_c = \tan \sin^{-1} \frac{x_0 + c}{R}$$

Chainage at 
$$h_{c:}$$
  $c = R. \sin \cos^{-1}(1 - \frac{h' - h_c}{R}) - x_0$  (14)

Chainage at 
$$i_{c}$$
:  $c = (R. \sin \cos^{-1} i_c) - x_0$  (15)

These equations apply to a reference surface - normally the rolling surface of the rail head. For any other surface, e.g. the underside of the rail flange or, in effect, the surfaces supporting the rail, increase or decrease, as appropriate, the curve radius, R by the offset between the two surfaces, normal to the surfaces at any point, and use this revised value, R' in (9) to (15).

In the case of rails or prefabricated beams supporting the rails, the applicable lengths are the arc lengths given in (12) and the relevant surface is the neutral axis of the rail or beam. The radius of curvature of

the ways is usually large enough, compared to the section depths that it is unnecessary to pre-form the sections. They will take up the curvature with a minimum of strain.

The trial profiles must be checked against a series of different vessels and of different stages of the tide to ensure that the target vessels can all be got onto the blocks at acceptable stages of the tide.

## 3.3. Other Curvature

Other vertical curves can be used, notably transitions from a straight grade to a vertical curve but they are only practical on two-point support which, depending on the capacity may involve articulated multiwheel carriages. This system is particularly applicable to side haul systems where the ways transition from inclined to level.

## 4. SUING A VESSEL

## 4.1. The Process of the Sue

The action of suing a vessel is the critical activity in dry docking a ship. It is the action of setting the ship down on the keel blocks. On a slipway it is the action of drawing the vessel up the ways on the cradle as she settles onto the blocks. (The word has the same origin as its legal usage being derived from the Latin meaning *to follow*).

The sue of a vessel begins with the first touch of one or other end of the keel on the keel blocks. The process of the sue is the process of lifting the vessel at this point of first touch, to rotate the vessel longitudinally, to change the apparent trim of the vessel until it is the same as the line of the keel blocks. The keel will then be in contact with the blocks along its full length. In principle, at this instant, the whole reaction between keel and blocks is still at the point of first touch and reaches a maximum value. But immediately, as the vessel continues to be lifted out, the increasing total load is spread out over all the blocks and the point sue load begins to diminish. Once the vessel is high and dry, the sue load disappears and the first touch or sue block only carries its fair share of the total load.

At first touch the marks at the sue end of the vessel will begin to rise out of the water. At the other end of the vessel the marks will, in general, sink into the water by about a third of the amount they rise at the sue end. When the keel touches fore and aft, the marks at the other end will cease to sink and begin to rise out of the water. It is just before and during this period that the vessel must be held in position to locate her correctly on the blocks.

## 4.2. Sue Loads

The significance of sue loading depends very much on the match between the vessel and the dry docking system.

Where the keel and keel blocks are very nearly parallel the sue loads will be very small and can be ignored. Where there is a large angle between the keel and the line of the keel blocks there will be a heavy sue and the docking of the vessel will be difficult.

## 4.3. Determination of Sue Load on Straight Grade Ways

Determining the magnitude of the sue load amounts to establishing the upwards force at one end of the keel needed to rotate the vessel longitudinally to change the trim of the vessel to match the slope of the keel blocks. Minikin (Minikin, R.R. 1963) suggests an allowance of between one eighth to one third of the displacement of the vessel. This gives excessive results and better values are needed.



Fig 11: The Sue of a Vessel

The traditional analysis of sue load is given in texts on naval architecture as launching or grounding calculations. To do this, the hydrostatic curves for the vessel are needed. In dry docking design work, these are not normally available.

A first approximation can be obtained by treating the vessel as a rectangular box (ignoring small angle effects at the vertical ends) and analysing the forces involved.



Fig 12: Sue of a Rectangular Box

This analysis of the sue load of the box in fig 12 gives:

$$S = \frac{1}{6} \Delta \frac{L_{BP}}{d} (i_b - i_k)$$
(16)

Although modern ship hull form is approximating more closely to that of a box – i.e. the block coefficient is increasing – a more detailed analysis is needed to take into account the fining of the lines of a real ship. This can be done by approximating all the hydrostatic curves by power functions. Using well-known approximations to typical ship form, the constants to the equations can be approximated by various combinations of block and water plane coefficients.

When the results are evaluated, they are very close to (16) and the sue load can be expressed as:

$$S = k.\Delta.\frac{\delta T}{d_m} \tag{17}$$

Where change in trim during the sue,  $\delta T$  is given by:

$$\delta T = L_{BP}(i_b - i_k) \tag{18}$$

and values of k are given in Table 1: Values of k.

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Block	Z – Ratio of Distance of Sue Point to Near Perpendicular tp L <sub>BP</sub>											
Coefficient C <sub>b</sub>	0	0.05	0.10	0.15	0.20	0.25	0.30					
0.3	0.18	0.19	0.21	0.23	0.26	0.29	0.33					
0.4	0.107	0.19	0.21	0.23	0.26	0.30	0.35					
0.5	0.17	0.19	0.21	0.23	0.26	0.31	0.37					
0.6	0.17	0.18	0.21	0.23	0.27	0.31	0.38					
0.7	0.17	0.18	0.20	0.23	0.27	0.32	0.39					
0.8	0.17	0.18	0.20	0.23	0.27	0.32	0.4					
1.0	0.17	0.19	0.21	0.24	0.28	0.33	0.42					

#### Table 1: Values of k

and

$$z = \frac{e \pm f}{L_{BP}} \tag{19}$$

The remaining symbols are as shown in Fig 8, Fig 10 and Fig 11

Draft at Sue Point at Full Sue:

Sue by the bow 
$$d_s = \frac{\Delta - S}{c_b \cdot L_{BP} \cdot B} - (\frac{L_{BP}}{2} - e + f)i_b$$
(20)

$$d_{s} = \frac{\Delta - S}{C_{b} \cdot L_{BP} \cdot B} + (\frac{L_{BP}}{2} - e - f)i_{b}$$
(21)

The critical points for the sue load are given by:

First touch: 
$$h_t = t - d_s - h_r$$
 (22)

Chainage of first touch:

$$c_t = c_1 + \frac{1 - c_1}{i_W} \tag{23}$$

(24)

Chainage at full sue

Sue by the stern

 $c_s = c_1 + \frac{h_1 - t + d_s + h_r}{i_w}$ 

Keel Dries when the stern is at:

$$c_d = c_1 + \frac{t - h_r}{i_w} \tag{25}$$

## 4.4. Sue on Vertically Curved ways

On vertically curved ways, the grade of the ways is constantly changing during the sue and the analysis becomes much more complex.

Using the same approach of approximating the hydrostatic curves by power functions, the following formulae have been established to compute the magnitude and position of the peak sue load:



Fig 13: Sue on Vertically Curved Ways

Slope of the keel at full sue

$$i_s = i_{bs} = \frac{|\sqrt{A^2 + B}| - A}{R}$$
 (26)

$$A = R.\,\varphi_b + q + K.\frac{d_f + d_a}{2} + \frac{1 - 2.z}{2}.\,L_{BP}$$
<sup>(27)</sup>

and

 $A = R. \varphi_b + q + K. \frac{d_f + d_a}{2} - \frac{1 - 2.Z}{2} L_{BP}$ (28)

 $B = 2.R \left[ h_1 + h_r - t + \frac{d_f + d_a}{2} \left( 1 + K \cdot \frac{d_a - d_f}{L_{BP}} \right) \right]$ (29)

Block	Z – Ratio of Distance of Sue Point to Near Perpendicular to $L_{BP}$ (19)											
Coefficient C <sub>b</sub>	0.00	0.05	0.10	0.15	0.20	0.25	0.30					
0.3	0.10	0.11	0.12	0.13	0.15	0.18	0.22					
0.4	0.10	0.12	0.13	0.15	0.16	0.20	0.24					
0.5	0.11	0.13	0.14	0.16	0.18	0.22	0.23					
0.6.	0.12	0.14	0.15	0.18	0.20	0.24	0.29					
0.7	0.13	0.15	0.16	0.19	0.22	0.26	0.32					
0.8	0.14	0.16	0.18	0.20	0.24	0.28	0.35					
0.9	0.15	0.18	0.19	0.22	0.26	0.31	0.38					
1.0	0.16	0.19	0.21	0.24	0.28	0.33	0.42					

Table 2: Values of K

## 5. KEEL BLOCK LOADING

Although the quality of the docking plans that are being provided with ships are improving, appropriate docking plans are commonly not available at a slipway design stage. The following procedures will provide an adequate assessment of the loading estimates needed for the structural design of the ways.

## 5.1. Average Keel Block Loading

Start the process with an assessment of the average keel block loading.



### Fig 14: Average Keel Block Loading

$$\omega = \frac{\Delta}{L_k} \tag{30}$$

#### 5.2. Parabolic Loading

In practice the load distribution on the keel is non-uniform and in general tends to an asymmetrical parabolic shape. (McSporran 2000) The position of the peak load will be off centre and its position must be made by estimation.



Fig 15: Parabolic Load distribution

The maximum load distribution is given by:

$$\omega_{max} = c.\,\omega\tag{31}$$

Unless better suggestions are available, use values of c as given in Table 3: Keel Block Load Factors

Type of Vessel	Constant c
Very stiff vessels, e.g. submarines	1.5
Stiff vessels e.g. tugs and trawlers	1.6
Medium stiff vessels e.g. freighters and container ships	1.75
Flexible vessels e.g. 'all aft' VLCC's and Cape Bulkers	1.8 – 1.9

#### Table 3: Keel Block Load Factors



Fig 16: Practical Load Assumption

### 5.3. Trapezoidal Loading

In general, the substructure of the ways is relatively stiff. With the usual flat, unsprung, cradle the combination will be quite rigid compared to even relatively stiff vessels and the parabolic load distribution as proposed here gives a reasonable load estimate. However, in some cases, particularly when the cradle is built up aft, the system substratum becomes much more flexible relative to stiff vessels. Under these conditions, the asymmetry of the loading becomes pronounced and the load distribution begins to approximate a trapezoidal form (McSporran 2000).

With a trapezoidal load distribution, estimating the position of the peak load intensity is no longer relevant. The key input is the position of the centre of weight of the vessel and whether it is within or without the middle third of the keel (Crandall 1967).



Centroid inside middle third



Centroid outside middle third

Fig 17: Trapezoidal Keel Block Load Distribution

Where the CG falls within the middle third, the minimum and maximum rates of loading are given by:

$$\omega_{min} = \omega \left( 1 - \frac{A}{B} \right) \tag{32}$$

$$\omega_{max} = \omega \left( 1 + \frac{A}{B} \right) \tag{33}$$

Where the CG falls outside the middle third, the effective length of keel blocks carrying load is given by:

$$L_{keff} = 1.5L_k - 3.A \tag{34}$$

and the maximum rate of keel block loading is given by:

$$\omega_{max} = 2.\,\omega\tag{35}$$

## 5.4. Lloyds Rules

Lloyds Rules (Lloyds Register 1981) have been developed for shiplifts but are applicable to slipways. Their load assessments are based on the parabolic method and they define two concepts:

Maximum Distributed Load (MDL): this is the maximum safe rate of loading on the keel blocks

Nominal Lifting Capacity (**NLC**): this is the maximum safe total lifting capacity of the cradle/ways system and is given by:

$$NLC = MDL x L_k x Distribution factor$$
 (36)

Lloyds allow a maximum distribution factor of 0.83 but normally they will not accept this higher value and limit the distribution factor to a maximum value of 0.67. This is equivalent a minimum value of c of 1.5 in **Table 3**.

## 6. WAYS LOADING – MINIKIN DIAGRAM

Minikin (Minikin R.R. 1963) described a method of plotting the variation of expected peak loading on the ways over the lifetime of the slipway. This is shown in **Fig 15: Minikin's Original Diagram** 



Fig 18: Minikin's Original Diagram

Given the procedures set out above, this diagram must be constructed from a montage of values for different vessels and different stages of the tide.

## 7. LATERAL SUPPORT FORCES

Ships are normally built symmetrical and balanced about the centreline. In the water they are normally trimmed to float on an even keel without any list to either side. In principle such a ship, dry docked, should balance on its keel without the need of any lateral support. Quite obviously, this would be a most dangerous practice but since the ship is balanced it is not at all clear what forces will be generated in the lateral support system.

Whatever the cause of overturning forces acting on a dry docked ship, they should be treated as overturning moments in order to calculate the forces acting on the support structures.

## 7.1. Transverse, (Wind) Forces

These occur when the vessel is high and dry and the normal procedures for wind loading on buildings apply. Lloyds (Lloyds Register 1981) propose a horizontal force of 2.5 kN/m<sup>2</sup> or a vertical loading at the outrigger ways or at the bilge suports equal to 20% of the keel loading.

## 7.2. Vessels with List or Loll

If a vessel is docked on the blocks heeled over at some small angle then it will topple over as it sues unless it is restrained by the lateral support structures – forces that will then be transmitted to the ways structures. As shown in **Fig 16**, the analysis depends on a knowledge of the lever arm  $l_a$  and this is difficult to determine. This condition is normally only found in smaller fishing vessels without adequate trimming tanks to bring the vessel back to upright. In general, an allowance of 5° of heel should be sufficient for design purposes.

In practice, vessels liable to cause such problems, will arrive heeled over at some small angle that it is not possible to correct before docking. This situation can be analysed by the principles of hydrostatics irrespective of whether it is the result of list or loll to yield the value of the overturning moment.

The overturning moment is given by:

$$M_{t} = [(c_{1}.L_{BP}.B^{3}) + (c_{2}.d_{m}.\Delta)] \tan \emptyset$$
(37)

#### Fig: 19 Overturning Moment

The values of the constants,  $c_1$  and  $c_2$  given in **Table 4: Overturning Moment Factors** have been given in terms of block coefficient although they are actually functions of the waterplane area coefficient, not the block coefficient. However, the block coefficient is usually much easier to obtain than the waterplane area coefficient and appropriate corrections have been made.

Cb	C1	C2
0.4	0.031	0.759
0.5	0.038	0.750
0.6	0.046	0.742
0.7	0.055	0.736
0.8	0.064	0.731
0.9	0.073	0.726
1.0	0.083	0.722

#### **Table 4: Overturning Moment Factors**

Equation (37) above gives an approximate, not an exact value but one which should be quite adequate for dry docking purposes.  $\phi$  is the angle of heel.

## 8. WAYS CONSTRUCTION

It is usual and economical to build slipway cradles without any suspension. In this respect they are akin to container cranes. Both require track that is set to extremely accurate levels. For container cranes, on the quayside, in the dry, this is not a difficult matter. Slipway rails underwater are a completely different matter. Extreme accuracy is required from the trade of marine construction underwater that is perhaps the roughest in the construction industry. Some ingenious engineering is required to marry these two.

Generally, a target accuracy better than  $\pm 1.5$  mm in level and  $\pm 3.0$  mm in line is adequate. To achieve this, very high accuracy levelling is needed. Where there is a reinforced concrete quay wall or jetty adjacent to the ways, parallax plate and invar staff levelling can be used. A chain of benchmarks will be needed and the highest level of accuracy is needed in surveying these. At this level of accuracy there will be some inconsistency in repeat measurements due to the tidal distortions of the earth's crust. Where suitable structures are not available some form of water tube levelling will be needed.

A 20 second construction theodolite will generally be sufficient to control the line of the ways.

## 8.1. Construction in the dry

Construction in the dry reverts to the sort of conventional construction used for container crane rails where it is relatively easy to achieve the required tolerances.

There are parts of the world with extreme tide ranges so that the ways can be constructed in the dry by working at low tide and only taking the ways down to spring low water. This is only really practical for smaller units and dry docking must take place as the tide rises.

Alternatively, the ways can be coffered so that work takes place in the dry. With proper geotechnical design, this is a very effective method but probably not the most economic.



Fig 20: 1200 ton Slipway Construction in the Dry, Port Elizabeth 1945 – Military Specs!

## 8.2. Prefabricated Construction



Fig 21: Construction Method for Slipway Ways ca 1895

Brysson Cunningham (Cunningham 1922) describes a method of construction used in 1895 to construct the 1500 ton slipway in East London, South Africa. The ways were still in good condition 100 years later although the facility had been decommissioned some years earlier. In this method, a crushed stone bed was levelled by trammel off prelevelled screed rails. The ways were assembled on pallets of timber and lowered on to the stone bed. See **Fig: 21** (Cunningham 1922).

For the construction of the 1200 ton slipway in Hobart, Tasmania, John Tubb (Tubb J.R. 1970) used load-bearing, prefabricated steel beams in 13 m long sections spanning between piled supports as the ways structure. See **Fig 22** and **Fig 23** (Tubb J.R. 1970) Each section, complete with rail and shuttering for encasing concrete, was template matched on land to the preceding section by means of  $\varphi$  76 mm (3 inch) pins in 0.8 mm (1/32 inch) clearance holes. The sections fitted precisely without any

discontinuity in the top surface between sections. Levelling for this project was done to an accuracy ± 1.5 mm. Accuracy of the final construction was probably somewhat coarser.



Fig 22: Prefabricated Steel Beam Ways



Loose bessian forming

ing top of pile . '' dia. stirrups

wo ?

Similar methods have been used with precast concrete elements for the ways structure. In general, these are not nearly as effective in meeting the tolerances. In the Saldanha Bay case, there were a number of discontinuities in the order of 25 mm (Mackie, K.P. 1970).

#### 8.3. **Incremental Launching**

The use of incremental launching of continuously cast concrete ways avoids the problem with joints. This is best done with precast concrete pedestals set to the required level, accuracy and head slope to receive the ways. Rollers can be attached to these pedestals to convey the ways with a 6 mm clearance and then removed when the launching is complete so that the ways settle onto the pedestals. The top of the ways provides the accurate surface for fixing the rails.

For small slipways, ways beams sufficient to carry the load will be light enough to launch over the pedestal rollers and be supported by the pedestals so that no further support is necessary. The only foundation needed is the foundation for the pedestals. For larger slipways a much more substantial structural support must be provided at rough tolerances by conventional construction. The control pedestals can then be set into these supports. The ways beam can be launched over this and encased off it to the required tolerances. In this case the ways beam is fairly insubstantial and serves only to provide an accurate surface for fixing the rails and transferring the loads to the more substantial substructure.

## 9. ANTI-FRICTION SYSTEMS

#### 9.1. **Greased Timber**

When ship sleds are used over greased timber the friction is in the order of 10%. Appropriate grease is a heavily graphited No 2 calcium grease i.e. bulldozer track grease.

#### 9.2. Wheels

Very small wheels, generally about  $\phi$  200 mm were used on the old patent slipways and they tended to crack like nuts (Tubb J.R. 1970). Friction, particularly with inaccurate track is in the order of 5% to 10%. More recently larger wheels of  $\phi$  300 mm to  $\phi$  350 mm have been used with the longitudinal members of the cradle steelwork resting on top of the axles. Friction is generally from 2% to 5%. With this arrangement the keel blocks are quite high above the rails necessitating longer ways.

An alternative is to use very large wheels,  $\phi$  600 or larger, and hang the longitudinal steelwork below the axles. With this arrangement, there is a significant reduction of the height of the keel blocks above the rails. With these large wheels, friction is < 1%.

It is normal practice to use plain bearings on slipway wheels. Appropriate grease is a No 2 lithium automotive grease or a heavily graphited No 2 calcium grease.

On a 200 ton slipway using the 3-way system, 100 no  $\phi$  300 wheels rated at 20 tons would have been needed. Using  $\phi$  600 underslung wheels rated at 32 tons on a 2-way system, only 16 no wheels were needed.

## Fig 24: φ 600 Underslung Wheel



## 9.3. Live Rollers

Common practice on railway dry docks is to use live roller trains instead of wheels but they can be used equally on slipways. Friction is commonly < 1%.

Like the wheel, these systems are basically very simple and robust but like the wheel there is a body of specialist knowledge needed to design and maintain them



Fig 25: Typical Live Roller Frame

## 10. Rails

Rails are characterised by the Hertz contact stresses between wheel and rail or between roller and plate. These reach their peak values below the contact surfaces where, even at a safe level, they can exceed the yield stress of the steel and are only safe to the extent that they are contained by the surrounding metal. Steel sections intended for rolling surfaces must have a minimum of section depth – hence the blocky design of a rail head. Provided adequate depth of section is maintained, design of rolling surfaces reverts to the structural issues of support of the load either by shear and bending where the rail spans between supports or by beam on elastic foundation theory where it has continuous support on the ways beam. The former only applies to flat bottom rails with sufficient I value to carry load in bending; the latter to either flat bottomed rails or to roller plates.

## 10.1. Fastening

Ideally no part of the fastenings should be cast into the concrete. All should be removable and replaceable to simplify rail maintenance. While various standardised, often patented rail clip systems are available, the attachment component is not. Inevitably this involves purpose designed attachments. After the corrosion effects on the rail itself, these are the most maintenance intensive component of system. Unfortunately, the class of person who commonly gets involved in this work, long after the construction has been completed, generally has no concept of the issues involved and lacks the nous

to have replicas of the relevant parts fabricated. By and large they all have one knee-jerk reaction: "drill baby drill" and use grouted-in bolts.

The answer is to join them and use properly designed, permanently fixed bolts. For durability these should be of stainless steel. However, the usual grades of 304 or 316 are not adequate. There are a number of more recent alloys that are much more appropriate and a competent stainless steel specialist should be consulted on the alloy selection.

With stainless steel bolts, they may not be allowed to come into contact with the reinforcement. Hence the bolts must be accurately placed. Cast-in bolts are not recommended. The upper surface of the ways beam needs to be steel floated to a fair flat surface and the templates needed to locate the bolts will interfere with the surface finishing. The bolts holes should be drilled into the concrete once it has set using a template to control the drilling. An appropriate proprietary bolt fixing system should be used to set the bolts into the holes in the concrete. The bolts must be set in to the correct depth so that heads of the bolts are at the correct level. Depending on the rail selection and cradle design, high bolts will foul the cradle. This is a common problem with bolts replaced underwater. The heads of the bolts are often set too high and are damaged by the cradle.

With stainless steel bolts it is vital that there is no electrical contact between the bolt and the rail. **Fig 26** is a suggest method of fixing the rails using UHMWPE as spacers and washers to isolate the stainless steel.



Fig: 26 Suggested Rail Fixing

## 10.2. Corrosion

Slipway rails exhibit pronounced Accelerated Low Water Corrosion (ALWC) although in the case of these rails, Microbially Induced Corrosion (MIC) does not appear to play any role. Rail corrosion is most intense just below low water springs. On flat bottom rails the weakest part is the thinnest, the web of the rail. With cathodic protection, this corrosion is suppressed below mid tide but becomes severe between mid and high tide. Generally, rails with thickened webs – in the order of 30 mm – should be used and all rails should be given a heavy duty anti corrosion coating.

Flat bottomed rails suffer from two other forms of corrosion, differential aeration cell corrosion and corrugation corrosion both focussed on the tidal zone particularly the lower tidal zone.

The differential aeration cell corrosion occurs in the lower tidal zone and only occurs on the lower end of the upper rail of a pair of rails joined by fishplates and is limited to a short length from the join. There seems to be an electro-chemical couple between the two ends and the head of the upper end of the lower rail is protected and shows no loss of metal. The simple cure is to use full penetration butt welded joins – either copper block welded or thermite welded.

The corrugation corrosion seems to be initiated by pitting corrosion in the rail head. Rolling work hardens the surface of the head outside the pits, changes its electro-chemical potential to more cathodic and sets up a couple between the work hardened metal and the metal in the pit. The effect is exacerbated by the natural frequency of the cradle. Cathodic protection will help.



Differential Aeration Cell Corrosion



Fig: 27 Differential Aeration Cell Corrosion

Slipway Rail

Corrugation Corrosion

Corrugations



**Fig 28 Corrugation Corrosion** 

The plate rolling surfaces needed for live roller trains seem to exhibit far less corrosion problems than flat bottomed rails.

## **11.CONCLUSION**

The above information, albeit abbreviated, gives a good overview of the complexity of slipway design and should provide a good companion to the design of a slipway and point the way to further investigations.

## 12. REFERENCES

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Cunningham, B. (1922) Principles and Practice of Dock Engineering (3<sup>rd</sup> ed) Charles Griffin London Lloyds Register (1981) Code for Lifting Appliances in a Marine Environment – Mechanical Lift Docks Mackie, K.P. (1970) Diagram of precise survey of the ways to the 1200 ton Saldanha Bay Slipway Mackie, K.P. (1979) Mechanical Systems of Dry Docking, University of Cape Town Mackie, K.P (2012) Manual of Basic Coastal & Harbour Engineering Mackie, K.P. (2016) Dry Dock Manual McSporran, R (2000) Analysis of Ships in Dry Docks, Thesis no 21, Dept of Civ. Eng., UCT Minikin, R.R. (1963) Winds, Waves and Maritime Structures, Charles Griffin London Munro-Smith, R (1967) Merchant Ship Design, Hutchinson Prosser, R.B. (1894) on Thomas Morton, Dictionary of National Biography, vol 39, Smith Elder, London Tubb, J.R. (1970) Some Aspects of the Design of Large Slipways, Proc ICE vol 46, May 1970

				APENDIX: Vertical	ly C	urve	d Wa	iys Ca	alculator - Formulae		
						SH	EET 1				
				Ways Curve Input					Ways Curve	Output	
Cell	Lable	Cell	Input	Description	Cell	Lable	Cell	Input			Description
G2	С <sub>1</sub>	H2	Input	Chainage at landward end (m)	P2	X,	Q2	=\$G4-\$	iF\$3	Distance from la	ndward to seaward end (m)
G3	C <sub>2</sub>	H3	Input	Chainage at seaward end (m)	P3	y'	Q3	=\$G\$5-	\$G\$6	Height landward	end above seaward end (m)
G4	h <sub>1</sub>	H4	Input	Level at landward end (m)	P4	α <sub>1</sub>	Q4	=ATAN	(\$G\$7)	Slope Angle at la	ind end (rad)
G5	h <sub>2</sub>	H5	Input	Level at seaward end (m)	P5	α2	Q5	=2*(ATAN(\$X\$4/\$X\$3))-\$X\$5 Slope Angle at sea end (rad)			ea end (rad)
G6	i <sub>1</sub>	H6	Input	Gradient at landward end (i in1)	P6	i <sub>2</sub>	Q6	=TAN(\$X\$6) Gradient at seaward er			vard end (i in 1)
G7	L <sub>c</sub>	H7	Input	Chord, ref block to cradle end (m)	P7	R	Q7	=\$X\$4/	((COS(\$X\$5))-(COS(\$X\$6)))	Radius of vertica	al curve (m)
G8	i <sub>bb</sub>	H8	Input	Build-up of blocks (i in 1)	P8	<b>X</b> 0	Q8	=(\$X\$8	*(SIN(\$X\$5)))-\$F\$3	Distance from c	rown to coord origin (m)
G9	δR	H9	Input	Height above or below ref surface (± m)	P9	h'	Q9	=\$G\$5-	+\$X\$8*(1-(COS(\$X\$5)))	Height of crown	above datum (m)
G10	Т	H10	Input	Maximum tide range (m)	P10	h <sub>r</sub>	Q10	=\$G\$12	2+\$G\$13	Block height abo	ve rail at reference point (m)
G11	w	H11	Input	Height of shim base above ref surface (m)	P11	R'	Q11	=\$X\$8-	-\$G\$10	Revised radius of	of vertical curve (m)
G12	b	H12	Input	Height of block above shim base (m)	P12	Х' <sub>0</sub>	Q12	=(\$X\$1	2*(SIN(\$X\$5)))-\$F\$3	Revised distance	e from crown to coord origin (m)
G13	L <sub>w</sub>	H13	Input	Length over keel blocks between block centres (m)	P13	h"	Q13	=\$G\$5-	+\$X\$12*(1-(COS(\$X\$5)))	Revised height c	f block above rail height at ref (m)
			W	ays Profile by Arc Length				Way	s Profile by Chainage		
	Repe	eat rov	v 19 for	further stations at other arc lengths from c1		R	epeat r	ow 19 fc	or further stations at other cha	ainages	
Cell	Lable	Cell		Input	Cell	Lable	Cell		Input		
B18	A	B19		Input arc length from c <sub>1</sub>	J18	С	J19		Input chainage from o	C <sub>1</sub>	
C18	Ca	C19	=\$X\$8*	(SIN((A19/\$X\$8)+\$X\$5))-\$X\$9	K18	A <sub>c</sub>	K19	=\$Y\$8*	((ASIN((\$Y\$9+#REF!)/\$Y\$8))	)-\$Y\$5)	
D18	h <sub>a</sub>	D19	=\$X\$10	)-\$X\$8*(1-COS(ASIN((\$X\$9+B19)/\$X\$8)))	L18	h <sub>c</sub>	L19	=\$Y\$10	\$Y\$8*(1-COS(ASIN((\$Y\$9+#REF!)/\$Y\$8)))		
E18	Ι <sub>Α</sub>	E19	=TAN(A	ASIN((\$X\$9+B19)/\$X\$8))	M18	I <sub>c</sub>	M19	=TAN(A	ASIN((\$Y\$9+#REF!)/\$Y\$8))		
				Vessel Data							
Cell	Input	Cell	Lable	Description				Input V	essel Data		
	Da	ta		Description	Cell	Input	Cell	Input	etc		
D34	1	E34	2		F34	3	G34	4	H34=5, I34=6 etc as needed		
D35	2	E35	Item		L	able ca	ases - se	elected o	lesign vessels - as needed		
D36	3	E36	L <sub>o/a</sub>	Length overall (m)			Input	Cols F, G	, H etc as needed		
D37	4	E37	L <sub>B/P</sub>	Length between perpendiculars (m)					do		
D38	5	E38	L <sub>k</sub>	Docking length of keel (m)					do		
D39	6	E39	Cb	Block coefficient					do		
D40	7	E40	c <sub>w</sub>	Waterplane coefficient					do		
D41	8	E41	Δ	Docking displacement (tons weight)					do		
D42	9	E42	d <sub>f</sub>	Draft fore (m)					do		
D43	10	E43	da	Draft aft (m)					do		
D44	11	E44	е	Offset of sue point from near perp, fore or aft (m)					do		
D45	12	E45	q	Offse of sue point from cradle reference point					do		
D46	13	E46	h <sub>r</sub>	Block height above rail at reference point (m)	1			Al	I=P10		
D47	14	E47	Т	Maximum tide range (m)				Al	=H10		

			APENDIX: Vertically Curved Wa	ays C	alcula	tor -	Formulae
<u> </u>			Sheet .	2			
Cell	Lable	Cell	Input Data	Cell	Lable	Cell	Computed Data
		B2		C4	R	C5	=Sheet1!\$Q\$7
C2	$L_{\alpha/\alpha}$	C3	= VLOOKUP(3, Sheet1!\$D\$34: Sheet1!\$N\$47, \$O\$5)	D4	Xo	D5	=Sneet1!\$Q\$8
D2	$L_{B/P}$	D3	=VLOOKUP(4,Sheet1!\$D\$34:Sheet1!\$N\$47,\$O\$5)	E4	h'	E5	=Sneet1!\$Q\$9
E2	L	E3	=VLOOKUP(5,Sheet1!\$D\$34:Sheet1!\$N\$47,\$O\$5)	F4	αı	F5	=Sheet1!\$Q\$4
F2	L	F3	=Sheet1!\$H\$7	G4	$\alpha_2$	G5	=Sheet1!\$Q\$5
G2	Cb	G3	=VLOOKUP(6,Sheet1!\$D\$34:Sheet1!\$N\$47,\$O\$5)	H4	C₁	H5	=Sheet1!\$H\$2
H2	Δ	H3	VLOOKUP(8,Sheet1!\$D\$34:Sheet1!\$N\$47,\$O\$5)	14	d_	15	=(J3+l3)/2
12	df	13	EVLOOKUP(9,Sheet1!\$D\$34:Sheet1!\$N\$47,\$O\$5)	J4	İhh	J5	=Sheet1!\$H\$8
J2	d <sub>a</sub>	J3	VLOOKUP(10,Sheet1!\$D\$34:Sheet1!\$N\$47,\$O\$5)	K4	h,	K5	=Sheet1!\$Q\$10
K2	j,	K3	=(J3-I3)/D3	L4	A <sub>b</sub>	L5	=2*\$C\$5*(ATAN((\$F\$3)/(2*(\$C\$5+\$L\$3))))
12	W	13	=Sheet1!\$H\$11	M4	i,	M5	=TAN(\$J\$5-ASIN((\$F\$3/(2*(\$C\$5+\$L\$3)))))
M2	b	M3	=Sheet1!\$H\$12	N4	i.	N5	=TAN(\$J\$5+ASIN((\$F\$3/(2*(\$C\$5+\$L\$3)))))
N2	Ť	N3	=Sheet1!\$H\$10		19	05	3
Coll	Labla	Coll	Intermediate Parameters	Coll	Labla	Coll	Sue Load Parameters
Cell	Lable	Cell	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18	Cell	Lable	Cell	Sue Load Parameters Output
Cell	Lable δt	Cell	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18	<b>Cell</b> C20	Lable δt	<b>Cell</b> C21	Sue Load Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31
Cell C7 D7 E7	<b>Lable</b> δt t	Cell C8 D8 F8	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 =\$C8*\$N\$3	Cell C20 D20	<b>Lable</b> δt t	<b>Cell</b> C21 D21	Sue Load Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31 =D8
C7 D7 E7	Lable δt t h <sub>r1f</sub>	Cell C8 D8 E8	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 =\$C8*\$N\$3 \$D8-\$I\$3-\$K\$5 \$D8-\$I\$3-\$K\$5	Cell C20 D20 E20	Lable δt t i <sub>st</sub>	Cell C21 D21 E21	Sue Load Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31 =D8 =(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8) =(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)
Cell C7 D7 E7 F7	Lable δt t h <sub>r1f</sub> h <sub>r1a</sub>	Cell C8 D8 E8 F8	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 =\$C8*\$N\$3 =\$D8-\$I\$3-\$K\$5 =\$D8-\$J\$3-\$K\$5 =\$D8-\$J\$3-\$K\$5-\$J\$5*\$F\$3 =\$C8C*\$K\$5-\$J\$5*\$F\$3	C20 D20 E20 F20	Lable δt t i <sub>sf</sub>	Cell C21 D21 E21 F21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08^2)-4*\$M8*\$P8)))/(2*\$M8)           < \$C\$C\$20(0.67)
C7 D7 E7 F7 G7	Lable δt t h <sub>r1f</sub> h <sub>r1a</sub> C <sub>r1f</sub>	Cell C8 D8 E8 F8 G8	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 =\$C8*\$N\$3 =\$D8-\$I\$3-\$K\$5 =\$D8-\$J\$3-\$K\$5-\$J\$5*\$F\$3 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5	Cell C20 D20 E20 F20 G20	Lable δt t i <sub>st</sub> n	Cell C21 D21 E21 F21 G21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08^2)-4*\$M8*\$P8)))/(2*\$M8)           =\$G\$37(-0.67)           < CD24 CVCE C (\$C\$E\$C\$C2
Cell C7 D7 E7 F7 G7 H7	<b>Lable</b> δt h <sub>r1f</sub> h <sub>r1a</sub> C <sub>r1f</sub> C <sub>r1a</sub>	Cell C8 D8 E8 F8 G8 H8	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 =\$C8*\$N\$3 =\$D8-\$J\$3-\$K\$5 =\$D8-\$J\$3-\$K\$5 =\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5	Cell C20 D20 E20 F20 G20 H20	Lable δt t i <sub>sf</sub> n h <sub>da</sub>	Cell C21 D21 E21 F21 G21 H21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           ≤(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08^2)-4*\$M8*\$P8)))/(2*\$M8)           =\$G\$37(-0.67)           ≤\$D21-\$K\$5-\$J\$5*\$F\$3           ∠(\$C\$C\$E_(\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C\$C
Cell C7 D7 E7 F7 G7 H7 T7	Lable	Cell C8 D8 E8 F8 G8 H8 H8 I8	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 =\$C8*\$N\$3 =\$D8-\$J\$3-\$K\$5 =\$D8-\$J\$3-\$K\$5-\$J\$5*\$F\$3 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5 =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5)) =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5))	C20 D20 E20 F20 G20 H20 I20	Lable δt i <sub>sf</sub> n h <sub>da</sub> C <sub>da</sub>	Cell C21 D21 E21 F21 G21 H21 I21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           ≤(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)           ≤(ABS(SQRT((\$08^2)-4*\$M8*\$P8)))/(2*\$M8)           ≤\$G\$37(-0.67)           ≤\$D21-\$K\$5-\$J\$5*\$F\$3           ≤(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$H21)/\$C\$5)))))-\$D\$5           ∠(1 + \$C\$0)/2)*(\$C02*\$CL\$22*\$CE\$24*\$CE
Cell C7 D7 E7 F7 G7 H7 17 J7	Lable $\delta t$ $h_{r1f}$ $h_{r1a}$ $C_{r1f}$ $C_{r1a}$ $A'_f$ $A'_a$	Cell C8 D8 E8 F8 G8 H8 H8 I8 J8	Intermediate Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18           =\$C8*\$N\$3           =\$D8-\$I\$3-\$K\$5           =\$D8-\$I\$3-\$K\$5           =\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5           =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5           =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5))	Cell C20 D20 E20 F20 G20 H20 I20 J20	Lable δt i <sub>sf</sub> n h <sub>da</sub> C <sub>da</sub> S <sub>f</sub>	Cell D21 E21 F21 G21 H21 I21 J21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08 <sup>2</sup> )-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08 <sup>2</sup> )-4*\$M8*\$P8)))/(2*\$M8)           =\$G\$37(-0.67)           =\$D21-\$K\$5-\$J\$5*\$F\$3           =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$H21)/\$C\$5)))))-\$D\$55           =((1+\$K8)/2)*(\$Q8*\$H\$33*\$E\$3*(\$E21-\$M\$5-\$K\$3)/\$I\$5)
C7 D7 E7 F7 G7 H7 I7 J7 K7	Lable	Cell C8 D8 E8 F8 G8 H8 H8 B 38 K8	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 =\$C8*\$N\$3 =\$D8-\$I\$3-\$K\$5 =\$D8-\$J\$3-\$K\$5-\$J\$5*\$F\$3 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5 =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5)) =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5)) =(\$L\$5-\$J8+\$I8)/ABS(\$L\$5-\$J8+\$I8) =(\$L\$5-\$J8+\$I8)/ABS(\$L\$5-\$J8+\$I8)	Cell C20 D20 E20 F20 G20 H20 I20 J20 K20	Lable δt i <sub>sf</sub> n h <sub>da</sub> C <sub>da</sub> S <sub>f</sub> S <sub>a</sub>	Cell C21 D21 E21 F21 G21 H21 I21 J21 K21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08^2)-4*\$M8*\$P8)))/(2*\$M8)           =\$G\$37(-0.67)           =\$SD21-\$K\$5-\$J\$5*\$F\$3           =(\$C\$\$5*(SIN(ACOS(1-((\$E\$5-\$H21)/\$C\$5)))))-\$D\$55           =((1+\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$E21-\$M\$5-\$K\$3)/\$I\$5)           =((1-\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$F21-\$M\$5-\$K\$3)/\$I\$5)
Cell C7 D7 E7 F7 G7 H7 T7 J7 K7 L7	Lable	Cell C8 D8 E8 F8 G8 H8 H8 B8 J8 K8 L8	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 =\$C8*\$N\$3 =\$D8-\$I\$3-\$K\$5 =\$D8-\$J\$3-\$K\$5-\$J\$5*\$F\$3 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5 =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5)) =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5)) =(\$L\$5-\$J8+\$I8)/ABS(\$L\$5-\$J8+\$I8) =1/((12*(\$C\$3*(-0.67))-1))	Cell C20 D20 E20 F20 G20 H20 I20 J20 K20 L20	$\begin{array}{c} \textbf{Lable} \\ \overline{\delta t} \\ t \\ i_{st} \\ i_{sa} \\ n \\ h_{da} \\ c_{da} \\ S_{f} \\ S_{a} \\ A_{r1f} \\ A_{r1f} \\ \end{array}$	Cell C21 D21 E21 F21 G21 H21 I21 J21 K21 L21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08^2)-4*\$M8*\$P8)))/(2*\$M8)           =\$G\$37(-0.67)           =\$S\$2^*(SIN(ACOS(1-((\$E\$5-\$H21)/\$C\$5)))))-\$D\$55           =((1+\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$E21-\$M\$5-\$K\$3)/\$I\$5)           =((1-\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$F21-\$M\$5-\$K\$3)/\$I\$5)           =\$C\$5*((ASIN((\$D\$5+\$G8)/\$C\$5)))-\$F\$5)
Cell C7 D7 E7 F7 G7 H7 H7 J7 K7 L7 K7	$      Lable \\ \overline{\delta t} \\ t \\ h_{r1f} \\ \overline{c}_{r1f} \\ \overline{c}_{r1a} \\ \overline{A}'_{f} \\ \overline{A}'_{a} \\ \overline{V} \\ \overline{K}' \\ \overline{A} \\ A$	Cell C8 D8 E8 F8 G8 H8 B8 J8 K8 K8 L8 M8	Intermediate Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18           =\$C8*\$N\$3         =\$C8*\$N\$3           =\$D8-\$I\$3-\$K\$5         =\$D8-\$J\$3-\$K\$5-\$J\$5*\$F\$3           =\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5           =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5           =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5))           =(\$L\$5-\$J8+\$I8)/ABS(\$L\$5-\$J8+\$I8)           =1/((12*(3-2*(\$G\$3^{(0.33))))+((\$G\$3^{(-0.67)})-1))           =\$C\$5*(AMEE/2) = \$L\$ \$P\$**55	Cell C20 D20 E20 F20 G20 H20 J20 K20 L20 M20	$\begin{array}{c} \textbf{Lable} \\ \overline{\delta t} \\ t \\ i_{sf} \\ i_{sa} \\ n \\ h_{da} \\ c_{da} \\ S_{f} \\ S_{a} \\ A_{r1f} \\ A_{r1a} \\ \end{array}$	Cell C21 D21 F21 G21 H21 I21 J21 K21 L21 M21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)           =\$G\$3^(-0.67)           =\$S\$2^(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$H21)/\$C\$5)))))-\$D\$55           =((1+\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$E21-\$M\$5-\$K\$3)/\$I\$5)           =((1-\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$F21-\$M\$5-\$K\$3)/\$I\$5)           =\$C\$5*((ASIN((\$D\$5+\$G8)/\$C\$5))-\$F\$5)           =\$C\$55*((ASIN((\$D\$5+\$H8)/\$C\$5))-\$F\$5)           =\$C\$55*((ASIN((\$D\$5+\$H8)/\$C\$5))-\$F\$5)
Cell C7 D7 E7 F7 G7 H7 H7 J7 K7 L7 M7 N7	Lable $\delta t$ $h_{r1f}$ $h_{r1a}$ $C_{r1f}$ $C_{r1a}$ $A'_f$ $A'_a$ V K' B	Cell C8 D8 E8 F8 G8 H8 B8 J8 K8 K8 L8 M8 N8	Intermediate Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18           =\$C8*\$N\$3         =\$C8*\$N\$3           =\$D8-\$J\$3-\$K\$5         =\$D8-\$J\$3-\$K\$5-\$J\$5*\$F\$3           ={\$C2\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5           ={\$C55*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5           =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5))           =\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5))           =\$C\$5*\$(ASIN((\$D\$5+\$H8)/\$C\$5))           =\$C\$5*\$(ASIN((\$D\$5+\$H8)/\$C\$5))           =\$C\$5*\$(ASIN((\$D\$5+\$H8)/\$C\$5))           =\$C\$5*\$(ASIN(\$D\$2+\$E\$83           =\$C\$5*\$(\$M\$5/2+\$L\$8*\$E\$3	Cell C20 D20 E20 F20 G20 H20 J20 K20 L20 M20 N20 N20	$\begin{array}{c} \textbf{Lable} \\ \overline{\delta t} \\ t \\ i_{sf} \\ i_{sa} \\ n \\ h_{da} \\ C_{da} \\ S_{f} \\ S_{a} \\ A_{r1f} \\ A_{r1a} \\ A_{sf} \\ A_{s$	Cell C21 D21 E21 F21 G21 H21 I21 J21 K21 L21 M21 N21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08^2)-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08^2)-4*\$M8*\$P8)))/(2*\$M8)           =\$G\$3^(-0.67)           =\$D21-\$K\$5-\$J\$5*\$F\$3           =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$H21)/\$C\$5)))))-\$D\$5           =((1+\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$E21-\$M\$5-\$K\$3)/\$I\$5)           =((1-\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$F21-\$N\$5-\$K\$3)/\$I\$5)           =\$C\$5*((ASIN((\$D\$5+\$G8)/\$C\$5))-\$F\$5)           =\$C\$5*((ASIN((\$D\$5+\$H8)/\$C\$5))-\$F\$5)           =((1+\$K8)/2)*(\$C\$5*((ATAN(\$E21))-\$F\$5)           =\$C\$5*((ASIN((\$D\$5+\$H8)/\$C\$5))-\$F\$5)           =((1+\$K8)/2)*(\$C\$5*((ATAN(\$E21))-\$F\$5)
Cell           C7           D7           E7           F7           G7           H7           J7           K7           L7           M7           N7           O7	Lable	Cell C8 D8 E8 F8 G8 H8 B8 J8 K8 K8 K8 L8 M8 N8 S8 S8 S8 S8 S8 S8 S8 S8 S8 S8 S8 S8 S8	Intermediate Parameters Output Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 =\$C8*\$N\$3 =\$D8-\$J\$3-\$K\$5 =\$D8-\$J\$3-\$K\$5-\$J\$5*\$F\$3 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5 =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5 =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5)) =\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5)) =(\$L\$5-\$J8+\$I8)/ABS(\$L\$5-\$J8+\$I8) =1/((12*(3-2*(\$G\$3^(0.33))))+((\$G\$3^(-0.67))-1))) =\$C\$5/2 =\$C\$5*\$M\$5/2+\$L\$8*\$E\$3 =\$C\$5*\$(\$M\$5/2)/2-\$E\$5-\$K\$5-\$I\$5+\$D8-(\$L8-0.5)*\$K\$3*\$E\$3 =\$C\$5*((\$M\$5^2)/2-\$E\$5-\$K\$5-\$I\$5+\$D8-(\$L8-0.5)*\$K\$3*\$E\$3	Cell C20 D20 E20 F20 G20 H20 I20 K20 L20 M20 N20 O20	Lable           δt           t           isa           n           h <sub>da</sub> C <sub>da</sub> S <sub>f</sub> S <sub>a</sub> A <sub>r1f</sub> A <sub>sf</sub> A <sub>ss</sub>	Cell C21 D21 E21 F21 G21 H21 I21 I21 K21 L21 M21 N21 O21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08/2)-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08/2)-4*\$M8*\$08)))/(2*\$M8)           =\$G\$37(-0.67)           =\$D21-\$K\$5-\$J\$5*\$F\$3           =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$H21)/\$C\$5)))))-\$D\$5           =((1+\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$E21-\$M\$5-\$K\$3)/\$I\$5)           =((1-\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$F21-\$N\$5-\$K\$3)/\$I\$5)           =\$C\$5*((ASIN((\$D\$5+\$G8)/\$C\$5))-\$F\$5)           =\$C\$5*((ASIN((\$D\$5+\$H8)/\$C\$5))-\$F\$5)           =((1+\$K8)/2)*(\$C\$5*((ATAN(\$E21))-\$F\$5)-\$L\$5/2)           =((1-\$K8)/2)*(\$C\$5*((ATAN(\$F21))-\$F\$5)-\$L\$5/2)
Cell           C7           D7           E7           F7           G7           H7           J7           K7           L7           M7           O7           P7           O7	$\begin{tabular}{c} Lable \\ \hline \delta t \\ t \\ h_{r1f} \\ h_{r1a} \\ C_{r1f} \\ C_{r1a} \\ A'_{f} \\ A'_{a} \\ V \\ K' \\ A \\ B \\ C_{f} \\ C_{a} \\ F \\ C_{a} \\ F \\ $	Cell C8 D8 E8 F8 G8 H8 B8 J8 K8 K8 L8 K8 K8 K8 K8 K8 K8 K8 K8 K8 K8 K8 K8 K8	Intermediate Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 $=$ \$C8*\$N\$3 $=$ \$D8-\$J\$3-\$K\$5 $=$ \$D8-\$J\$3-\$K\$5 $=$ \$S8 $=$ \$C\$5*(SIN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5 $=$ \$(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5 $=$ \$(\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5)) $=$ \$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5)) $=$ \$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5)) $=$ \$C\$5*(\$M\$5/2+\$L\$8*\$E\$3 $=$ \$C\$5*(\$M\$5/2+\$L\$8*\$E\$3 $=$ \$C\$5*(\$M\$5/2)/2-\$E\$5-\$K\$5-\$I\$5+\$D8-(\$L8-0.5)*\$K\$33*\$E\$3 $=$ \$C\$5*(\$N\$5/2)/2-\$E\$5-\$K\$5-\$I\$5+\$D8+(\$L8-0.5)*\$K\$33*\$E\$3	Cell C20 D20 E20 F20 G20 H20 H20 H20 L20 K20 L20 M20 N20 O20 P20	$\begin{array}{c} \textbf{Lable} \\ \overline{\delta t} \\ t \\ i_{sf} \\ n \\ h_{da} \\ C_{da} \\ S_{f} \\ S_{a} \\ A_{r1f} \\ A_{r1a} \\ A_{sf} \\ A_{sa} \\ A_{da} \\ A_{d$	Cell C21 D21 E21 F21 G21 H21 I21 I21 K21 L21 K21 N21 O21 P21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08'2)-4*\$\M8*\$08)))/(2*\$\M8)           =(ABS(SQRT((\$08'2)-4*\$\M8*\$08)))/(2*\$\M8)           =\$G\$3'(-0.67)           =\$D21-\$K\$5-\$J\$5*\$F\$3           =(\$C\$\$5*(SIN(ACOS(1-((\$E\$5-\$H21)/\$C\$5)))))-\$D\$5           =((1+\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$E21-\$M\$5-\$K\$3)/\$I\$5)           =((1+\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$F21-\$N\$5-\$K\$3)/\$I\$5)           =\$C\$5*((ASIN((\$D\$5+\$G8)/\$C\$5))-\$F\$5)           =\$C\$5*((ASIN((\$D\$5+\$H8)/\$C\$5))-\$F\$5)           =((1+\$K8)/2)*(\$C\$5*((ATAN(\$E21))-\$F\$5)-\$L\$5/2)           =((1-\$K8)/2)*(\$C\$5*((ATAN(\$F21))-\$F\$5)-\$L\$5/2)           =((1-\$K8)/2)*(\$C\$5*((ATAN(\$F21))-\$F\$5)-\$L\$5/2)
Cell           C7           D7           E7           G7           H7           J7           K7           L7           M7           O7           P7           Q7	$\begin{tabular}{c} Lable \\ \hline \delta t \\ t \\ h_{r1f} \\ h_{r1a} \\ C_{r1fa} \\ C_{r1a} \\ A'_{f} \\ A'_{a} \\ V \\ K' \\ A \\ B \\ C_{f} \\ C_{a} \\ K \end{tabular}$	Cell           C8           D8           E8           F8           G8           H8           J8           K8           L8           M8           N8           O8           P8           Q8	Intermediate Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C8 to C18 $=$ \$C8*\$N\$3 $=$ \$D8-\$J\$3-\$K\$5 $=$ \$D8-\$J\$3-\$K\$5 $=$ \$D8-\$J\$3-\$K\$5 $=$ \$C8*\$IN(ACOS(1-((\$E\$5-\$E8)/\$C\$5)))))-\$D\$5 $=$ \$(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$F8)/\$C\$5)))))-\$D\$5 $=$ \$(\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5))) $=$ \$\$C\$5*(ASIN((\$D\$5+\$G8)/\$C\$5)) $=$ \$\$C\$5*(ASIN((\$D\$5+\$H8)/\$C\$5)) $=$ \$\$C\$5*(ASIN((\$D\$5/2+\$L\$8*\$E\$3) $=$ \$C\$5*(\$M\$5/2+\$L\$8*\$E\$3 $=$ \$C\$5*(\$M\$5/2)/2-\$E\$5-\$K\$5-\$I\$5+\$D8-(\$L8-0.5)*\$K\$3*\$E\$3 $=$ \$C\$5*(\$N\$5/2)/2-\$E\$5-\$K\$5-\$I\$5+\$D8+(\$L8-0.5)*\$K\$3*\$E\$3 $=$ \$L8*\$G\$3'(-0.67)	Cell C20 D20 E20 F20 G20 H20 I20 K20 L20 K20 L20 M20 O20 P20 Q20	Lable $\delta t$ $i_{sf}$ $i_{sa}$ $n$ $h_{da}$ $C_{da}$ $S_f$ $S_f$ $A_{r1f}$ $A_{sa}$ $A_{da}$ $A_{da}$ $A_{max}$	Cell C21 D21 E21 F21 G21 H21 I21 I21 K21 L21 K21 N21 O21 P21 Q21	Sue Load Parameters           Output           Repeat input fraction of tide e.g. 0 to 1 x 0.1 in C21 to C31           =D8           =(ABS(SQRT((\$08/2)-4*\$M8*\$08)))/(2*\$M8)           =(ABS(SQRT((\$08/2)-4*\$M8*\$08)))/(2*\$M8)           =\$G\$37(-0.67)           =\$D21-\$K\$5-\$J\$5*\$F\$3           =(\$C\$5*(SIN(ACOS(1-((\$E\$5-\$H21)/\$C\$5)))))-\$D\$5           =((1+\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$E21-\$M\$5-\$K\$3)/\$I\$5)           =((1+\$K8)/2)*(\$Q8*\$H\$3*\$E\$3*(\$F21-\$N\$5-\$K\$3)/\$I\$5)           =\$C\$5*((ASIN((\$D\$5+\$G8)/\$C\$5))-\$F\$5)           =\$C\$5*((ASIN((\$D\$5+\$H8)/\$C\$5))-\$F\$5)           =((1+\$K8)/2)*(\$C\$5*((ATAN(\$E21))-\$F\$5)-\$L\$5/2)           =((1+\$K8)/2)*(\$C\$5*((ATAN(\$F21))-\$F\$5)-\$L\$5/2)           =((1+\$K8)/2)*(\$C\$5*((ATAN(\$F21))-\$F\$5)-\$L\$5/2)           =((1-\$K8)/2)*(\$C\$5*((ATAN(\$F21))-\$F\$5)-\$L\$5/2)           =((1-\$K8)/2)*(\$C\$5*((ATAN(\$F21))-\$F\$5)-\$L\$5/2)

t = tide (m)  $i_{sf} = Grade of rail fore at full sue$ 

 $A_{da}$  = Arc distance from datum to end of cradle

A<sub>max</sub> = Arc distance from datum of max load

h<sub>da</sub> = Height of rail at aft end of cradle when keel dries (m)

 $c_{da}$  = Chainage of rail at aft end of cradle when keel dries (m)

 $A_{r1f}$  = Arc distance from datum to ref point at 1<sup>st</sup> touch fore (m)

A<sub>r1a</sub> = Arc distance from datum to aft end of cradle at 1<sup>st</sup> touch aft (m)  $A_{sa}$  = Arc distance from datum to point of full sue aft (m)

 $A_{sf}$  = Arc distance from datum to point of full sue fore (m)

 $S_f = Full sue fore(t)$  $S_a = Full sue aft (t)$